

9-21-15

### Systems of Equations and Inequalities Word Problems

Key Words or Phrases:

**sum** - means add**difference** - means subtract**less than** - means subtract**more than** - means add**twice or double** - means multiply by 2**product** - means multiply**quotient** - means divide**is** - means equals**1/2 of, 1/3 of, 2/5 of** -- means multiply by that fraction**minimum** - means greater than or equal to**maximum** - means less than or equal to**at least** - means greater than or equal to**at most** - means less than or equal to**no more** - means less than or equal to

Sep 23-12:37 PM

Sep 28-4:56 PM

The difference of two numbers is 7

$$x - y = 7$$

The cost, C, of a tv is equal to the price, P, plus tax, T.

$$C = P + T$$

She has no more than 50 pairs of shoes

$$x \leq 50$$

The number of boys is at least twice the number of girls

$$B \geq 2G$$

5. Erin is buying hamburgers and hotdogs for a party. She needs to buy a minimum of 30 items, but does not want to exceed 70 items. She also decides the number of hamburgers should be at least 3 times the number of hotdogs. Write a system of inequalities for the situation.

$$\begin{aligned} HM + HD &\geq 30 \\ HM + HD &\leq 70 \\ HM &\geq 3HD \end{aligned}$$

Sep 29-8:22 AM

Sep 29-10:17 AM

**STEPS IN SOLVING WORD PROBLEMS WITH LINEAR EQUATIONS & INEQUALITIES**

1. Define the variables that you want to find with let statements.
2. Create equations or inequalities that express the information given in the problem's scenario.
3. Solve your system using algebraic methods (graphing, substitution, or elimination).
4. Consider if your answer is reasonable.
5. Label your solution appropriately.
6. Check your answer with the conditions given in the problem.

6. The admission fee at a small fair is \$1.50 for children and \$4.00 for adults. On a certain day, 2200 people enter the fair and \$5050 is collected. How many children and how many adults attended?

Step 1: Define the variables.  
Let  $a$  = the number of adults; let  $c$  = the number of children

Step 2: Create equations.

$$\begin{array}{r} \$ \quad 1.50c + 4.00a = 5050 \\ \# \quad -4(c + a = 2200) \end{array}$$

$$\begin{array}{r} 1.50c + 4.00a = 5050 \\ -4.00c - 4.00a = -8800 \\ \hline -2.50c = -3750 \\ \underline{-2.50} \quad \underline{-2.50} \\ c = 1500 \end{array}$$

$$\begin{array}{r} 2200 \\ -1500 \\ \hline a = 700 \end{array}$$

Step 3: Solve the system.

Step 4: Is your answer reasonable?

Step 5: Label solutions.

Step 6: Check answer.

Sep 23-12:34 PM

Sep 23-12:37 PM

9. An exam worth 145 points contains 50 questions. Some of the questions are worth two points and some are worth five points. How many two point questions are on the test? How many five point questions are on the test?

Step 1: Define variables.  
Let  $x$  = the number of 2-point questions; let  $y$  = the number of 5-point questions

Step 2: Create equations.

$$\begin{array}{l} \text{Question} \quad 2(x + y = 50) \\ \text{Points} \quad 2x + 5y = 145 \end{array}$$

$$\begin{array}{r} -2x - 2y = -100 \\ 2x + 5y = 145 \\ \hline 3y = 45 \\ \underline{30} \quad \underline{3} \\ y = 15 \end{array}$$

Step 3: Solve the system.

$$\begin{array}{r} 50 \\ -15 \\ \hline 35 \end{array}$$

3 2pt ?s    15 5pt ?s

Step 4: Is your answer reasonable?

Step 5: Label solutions.

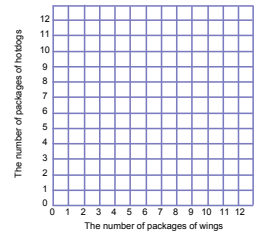
Step 6: Check answer.

7. Jason is buying wings and hotdogs for a party. One package of wings costs \$7. One package of hotdogs costs \$4. He knows that he will buy at least 5 packages of hotdogs. How many packages of each can he buy if he must spend less than \$40?

Step 1: Define variables.

Step 2: Create inequalities.

Step 3: Solve the system.



Step 4: Is your answer reasonable?

Step 5: Label solutions.

Step 6: Check answer.

Sep 23-12:51 PM

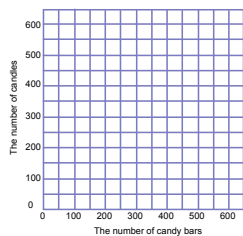
Sep 23-12:51 PM

8. The boys' and girls' soccer teams are trying to raise money for new uniforms. The boys' soccer team is selling candy bars for \$2 and the girls' soccer team is selling candles for \$4. They must raise more than \$800. The girls expect to sell at least 100 candles. How many candy bars and candles could be sold to raise the \$800?

Step 1: Define variables.

Step 2: Create inequalities.

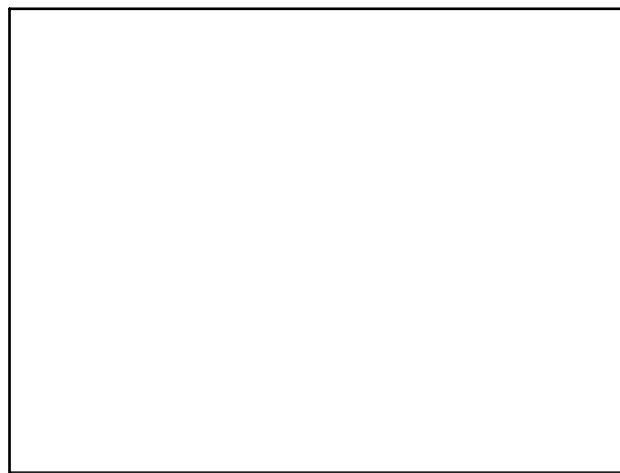
Step 3: Solve the system.



Step 4: Is your answer reasonable?

Step 5: Label solutions.

Step 6: Check answer.



Sep 23-12:51 PM

Sep 21-10:03 AM