

WARMUP 1-26-15

Find the value.

1. $\sin \frac{7\pi}{6} = -\frac{1}{2}$
2. $\cos \frac{2\pi}{3} = -\frac{1}{2}$
3. $\tan \frac{\pi}{4} = 1$

55, 61, 59, 57

$$C(x) = 800 - 10x + 0.25x^2$$

2.2 Polynomial Functions

$x = 20$ fixtures
 $y = 700$

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Jan 23-8:13 PM

The graphs of polynomial functions are smooth & continuous, whose domains are $(-\infty, \infty)$.
(In calculus, we have functions with these characteristics.)

Polynomial Functions

Nonpolynomial Functions

3 Important Aspects of Polynomial Functions:

- 1) End behavior
- 2) Zeros x -int
- 3) Relative extrema (min's and max's)

The coolest part ::

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Jan 13-5:06 PM

Identifying Degree and Leading Coefficient

- Degree of a polynomial: the highest power .
- Leading coefficient: the number in front of the term with the highest power

$$-4x^5 + 5x^3 + 8x^2 + 3x - 17$$

$$5x^3 + 8x^2 + 3x - 17 - 4x^5$$

Degree: 5
 Leading Coefficient: -4

Note: If your degree is k, then your polynomial has at most k zeros

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Common Polynomial Functions

Degree	Type	Example
0	constant	$f(x) = c$
1	linear	$f(x) = x$
2	quadratic	$f(x) = x^2$
3	cubic	$f(x) = x^3$
4	quartic	$f(x) = x^4$

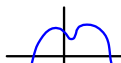
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End Behavior :: What happens as...

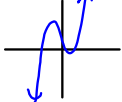
Even Degree
Lead Coefficient (+)



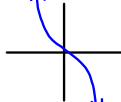
Even Degree
Lead Coefficient (-)



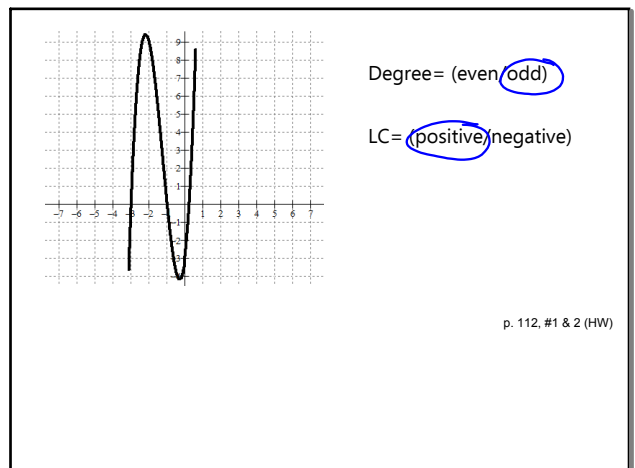
Odd Degree
Lead Coefficient (+)



Odd Degree
Lead Coefficient (-)



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Describe the end behavior for each function. Sketch the graph.

$f(x) = -3x^4 + 5x^2 + 1$ As $x \rightarrow \infty$, $f(x) \rightarrow -\infty$ As $x \rightarrow -\infty$, $f(x) \rightarrow -\infty$	$h(x) = -x^3 + 5x^2 + 1$ As $x \rightarrow \infty$, $f(x) \rightarrow -\infty$ As $x \rightarrow -\infty$, $f(x) \rightarrow \infty$
$g(x) = 2x^5 + x^4 - x^2 + 1$ As $x \rightarrow \infty$, $f(x) \rightarrow \infty$ As $x \rightarrow -\infty$, $f(x) \rightarrow -\infty$	$k(x) = x^2 + 6x - 7$ As $x \rightarrow \infty$, $f(x) \rightarrow \infty$ As $x \rightarrow -\infty$, $f(x) \rightarrow \infty$

Finding Real Zeros

Real zero :: Zeros, Solutions, factored, x-int.

Multiplicity :: $(x+4)^2$
 Repeated Zero {Bounce}

FACTOR!FACTOR!FACTOR!FACTOR!FACTOR!FACTOR!

Jan 24-11:26 PM

Nov 12-11:03 AM

Some Factoring Review...

Greatest Common Factor $4x^3 + 16x^2 - 24x$ $4x(x^2 + 4x - 6)$

Difference of Squares $x^2 - 64$ $(x-8)(x+8)$

Trinomial Factorization $x^2 + 8x + 12$ $(x+6)(x+2)$

Quadratic in Form $x^4 + 8x^2 + 12$ $(x^2+6)(x^2+2)$

Factor by Grouping $5x^3 - 15x^2 - 2x + 6$
 $5x^2(x-3) - 2(x-3)$
 $(x-3)(5x^2-2)$

p. 113, #29 (HW)

Example

Find all the real zeros of the polynomial function. Determine the multiplicity of each zero.

$f(x) = x^2 - 16$ $(x-4)(x+4)$ $x-4=0$ $x+4=0$ $x=4$ $x=-4$ Mult of 1	$f(x) = x^2 + 10x + 25$ $(x+5)(x+5)$ $x=-5$ Mult of 2	$f(x) = x^3 + 2x^2 + x$ $x(x^2 + 2x + 1)$ $x(x+1)(x+1)$ $x=0$ $x=-1$ Mult 1 Mult 2
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p. 113, #23 (HW)

Jan 14-8:28 PM

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A **zero** is a number you put in for x that makes $f(x)$ zero.

If the polynomial function $f(x) = x^2 + 9x + 20$
can be factored into $f(x) = (x+4)(x+5)$

what are the function's zeros?

$$x = -4 \quad x = -5$$

REVERSE//If a polynomial has zeros 2 & -1, what are its linear factors?

$$(x-2)(x+1)$$

$$x^2 + x - 2x - 2$$

$$f(x) = x^2 - x - 2$$

Jan 13-10:19 AM

Example

Find the polynomial in standard form given zeros: 4, -3, 0.

$$f(x) = x(x-4)(x+3)$$

$$f(x) = x^3 - x^2 - 12x$$

p. 113, #51 (HW)

Jan 14-8:42 PM

HOMework

...you can breathe! We're back to algebra!

p. 112 :: 1-8, 15, 17, 23, 29, 37, 39, 41, 51, 67, 69, 91

Jan 14-8:43 PM