

Polar Coordinates and graphing of polar equations due Tomorrow. (3 Assignments)



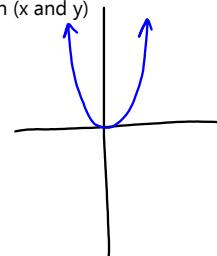
9.5: Parametric Equations

Before...

"**rectangular equations**"

equations that only describe position (x and y)

$$y = x^2$$



Dec 19-1:21 PM

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Now...

"**parametric equations**"

equations that describe position (x and y) AND time (t)

$$x = t$$

$$y = t^2$$

Parametric Equations introduce a 3rd variable or **parameter**.

Parametric equations are useful in modeling **curvilinear motion** which describes the path of an object in terms of space (**position**) and **time**.

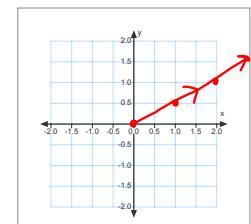
Orientation of a curve results from plotting (x,y) points based on **increasing** values of t.

Ex. Define the path of the object and describe orientation given parametric equations:

$$\Rightarrow x=t$$

$$\Rightarrow y=\frac{1}{2}t$$

t	0	1	2	3
x	0	1	2	3
y	0	$\frac{1}{2}$	1	$\frac{3}{2}$



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Dec 19-9:47 AM

How to Eliminate the Parameter t
p. 705, #11 (HW)

We eliminate the parameter to identify the object's path or curve.

- ① Solve for t.
- ② Plug in t = ...

Ex. Sketch the curve by eliminating the parameter.

$x = \sqrt{t}$

$y = 1 - t$

$x = \sqrt{t}$

$x^2 = t$

$y = 1 - x^2$

Confirm with calc:
Nspire - Menu/Graph Type/Parametric
TI-84 - Mode/PAR

How to Eliminate the Parameter θ (angle)
p. 705, #11 (HW)

Useful for modeling circular movement.

- ① Solve for cos θ and/or sin θ
- ② Plug into $\cos^2 \theta + \sin^2 \theta = 1$

$$x^2 + \left(\frac{y}{4}\right)^2 = 1$$

$$x^2 + \frac{y^2}{16} = 1$$

Ex. Sketch the curve by eliminating the parameter.
What do we call this shape?

$x = \cos \theta$ $\cos \theta = x$

$y = 4 \sin \theta$ $\sin \theta = \frac{y}{4}$

Confirm with calc:
Nspire - Menu/Graph Type/Parametric
TI-84 - Mode/PAR

plot where $0 < \theta \leq 2\pi$
(default in calculator)

Dec 19-10:10 AM

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HOMEWORK

parameters!
Get ready for Bug Races on Monday!!!!

9.5 (p. 705): 1-5 (odd), 11-21 (odd), 22, 36, 49, 66

Just a reminder of CONIC SECTIONS...

Dec 19-3:09 PM

Jan 6-8:52 PM