

Calculus Preview :: Function Decomposition and Difference Quotient

1 - 5: For each of the following functions $h(x)$, determine $f(x)$ and $g(x)$ such that $h(x) = (f \circ g)(x)$.

1. $h(x) = \sqrt{x^2 - 2}$ $f(x) = \underline{\hspace{2cm}}$

Check: $(f \circ g)(x) = \underline{\hspace{2cm}}$

2. $h(x) = (5x + 7)^2$ $f(x) = \underline{\hspace{2cm}}$

Check: $(f \circ g)(x) = \underline{\hspace{2cm}}$

3. $h(x) = \frac{1}{4x^3 + 1}$ $f(x) = \underline{\hspace{2cm}}$

Check: $(f \circ g)(x) = \underline{\hspace{2cm}}$

4. $h(x) = (x - 5)^{\frac{3}{2}}$ $f(x) = \underline{\hspace{2cm}}$

Check: $(f \circ g)(x) = \underline{\hspace{2cm}}$

5. $h(x) = 4^{x^2 - 9}$ $f(x) = \underline{\hspace{2cm}}$

Check: $(f \circ g)(x) = \underline{\hspace{2cm}}$

6 - 7: Let $f(x) = 5x + 3$ and $g(x) = x + h$

6. Find $f(g(x))$ $f(g(x)) = \underline{\hspace{2cm}}$

7. Find $\frac{f(x+h)-f(x)}{h}$ $\frac{f(x+h)-f(x)}{h} = \underline{\hspace{2cm}}$

8 - 10: Let $f(x) = x^2 + 3x + 1$

8. Find $f(7)$ $f(7) = \underline{\hspace{2cm}}$

9. Find $f(x + h)$ $f(x + h) = \underline{\hspace{2cm}}$

10. Find $\frac{f(x+h)-f(x)}{h}$ $\frac{f(x+h)-f(x)}{h} = \underline{\hspace{2cm}}$