

35, 79, 47, 55

$$\frac{5+0i}{2+2i}$$

$$\begin{aligned} V_1 &= 5 \operatorname{cis} 0^\circ & r_1 &= \sqrt{5^2 + 0^2} = 5 \\ V_2 &= 2\sqrt{2} \operatorname{cis} 45^\circ & \theta_2 &= \tan^{-1}\left(\frac{0}{5}\right) = 0^\circ \\ & & r_2 &= \sqrt{2^2 + 2^2} = \sqrt{8} = 2\sqrt{2} \\ & \frac{5}{2\sqrt{2}} \operatorname{cis}(0-45^\circ) & \theta_3 &= \tan^{-1}\left(\frac{2}{2}\right) = 45^\circ \\ & \cancel{\frac{5}{2\sqrt{2}} \left(\cos(-45^\circ) + i \sin(-45^\circ) \right)} \\ & \cancel{\frac{5}{2\sqrt{2}} \left(\frac{\sqrt{2}}{2} - \frac{\sqrt{2}}{2}i \right)} \\ & \frac{5}{4} - \frac{5}{4}i \end{aligned}$$

$$z = r(\cos \theta + i \sin \theta) \quad z = r (\cos \theta + i \sin \theta)$$

$$\begin{aligned} z^2 &= r^2 (\cos(2\theta) + i \sin(2\theta)) \\ z^3 &= r^3 (\cos(3\theta) + i \sin(3\theta)) \end{aligned}$$

$$z^6 = r^6 \operatorname{cis}(6\theta)$$

$$z^n = r^n \operatorname{cis}(n\theta)$$

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Steps for using Mr. Abraham's DeMoivre's Theorem:

$$z^n = r^n (\operatorname{cis}(n\theta))$$

Example 6 p. 452Use DeMoivre's Theorem to find $(-1 + \sqrt{3}i)^{12}$

$$\begin{aligned} z^{12} &= 2^{12} \left(\operatorname{cis} 12(120^\circ) \right) \\ z^{12} &= 4096 \left(\operatorname{cis} 1440^\circ \right) \end{aligned}$$

p. 458, #91 (HW)

$$\begin{aligned} r &= \sqrt{(-1)^2 + (\sqrt{3})^2} = 2 \\ \theta &= \tan^{-1}\left(\frac{\sqrt{3}}{-1}\right) + 180^\circ \\ \theta &= 120^\circ \end{aligned}$$

Roots of Complex Numbers

Fundamental Theorem of Algebra:

of solutions is equal to the degree.

$$\begin{aligned} \sqrt[4]{x^4} &= \pm 1 \\ x &= \pm 1 \end{aligned}$$

Double
Roots

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Dec 5-4:05 PM

Can we find a formula that gives us ALL the roots?

nth Roots of a Complex Number

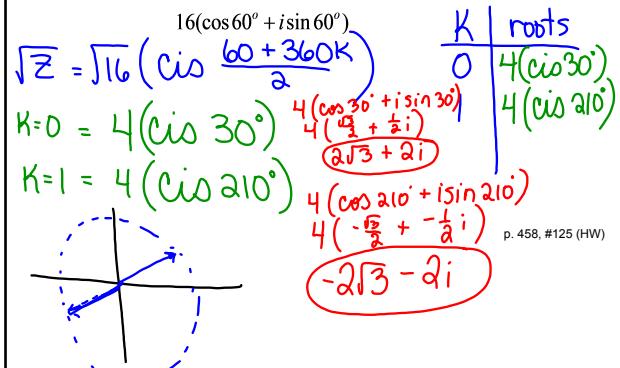
The nth roots of a complex number $z = r(\cos\theta + i\sin\theta)$ are given by:

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\text{cis } \frac{\theta + 360K}{n} \right)$$

where $k=0, 1, 2, \dots, n-1$

Example p. 458, #126

(a) Find the square roots of the given complex number, (b) represent each of the roots graphically, and (c) write each of the roots in standard form.



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Example 8 p. 455

Find the three cube roots of $z = -2 + 2i$

$$\begin{aligned} \sqrt[3]{z} &= \sqrt[3]{\sqrt{8}} \left(\text{cis } \frac{135 + 360K}{3} \right) \\ R &= \sqrt{(-2)^2 + (2)^2} = \sqrt{8} \\ \theta &= \tan^{-1}\left(\frac{2}{-2}\right) + 180^\circ = 135^\circ \\ \text{Roots} &= \sqrt[3]{\sqrt{8}} \cdot \text{cis } 45^\circ, \sqrt[3]{\sqrt{8}} \cdot \text{cis } 165^\circ, \sqrt[3]{\sqrt{8}} \cdot \text{cis } 285^\circ \end{aligned}$$

p. 458, #129 (HW)

HOMEWORK

...due Monday along with 6.5a and 6.4-6.5 Partner Quiz

6.5b (p. 458): 91-105 (odd), 113, 115, 125-131 (odd), 141, 143

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Dec 4-3:18 PM