

35, 79, 47, 55

$$\frac{5+0i}{2+2i}$$

$V_1 = 5 \operatorname{cis} 0^\circ$
 $V_2 = 2\sqrt{2} \operatorname{cis} 45^\circ$
 $\frac{5}{2\sqrt{2}} \operatorname{cis} (0-45)$
 $\frac{5}{2\sqrt{2}} (\cos(-45^\circ) + i \sin(-45^\circ))$
 $\frac{5}{2\sqrt{2}} (\frac{\sqrt{2}}{2} - \frac{\sqrt{2}}{2}i)$
 $\frac{5}{4} - \frac{5}{4}i$

$r_1 = \sqrt{5^2 + 0^2} = 5$
 $\theta_1 = \tan^{-1}(\frac{0}{5}) = 0^\circ$
 $r_2 = \sqrt{2^2 + 2^2} = 2\sqrt{2}$
 $\theta_2 = \tan^{-1}(\frac{2}{2}) = 45^\circ$

$z = r(\cos \theta + i \sin \theta)$ $z = r(\operatorname{cis} \theta)$
 $z^2 = r^2(\cos(2\theta) + i \sin(2\theta))$
 $z^3 = r^3(\cos(3\theta) + i \sin(3\theta))$
 $z^6 = r^6 \operatorname{cis}(6\theta)$
 $z^n = r^n \operatorname{cis}(n\theta)$

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Steps for using Mr. Abraham's DeMoivre's Theorem:

$$z^n = r^n (\operatorname{cis}(n\theta))$$

Example 6 p. 452
Use DeMoivre's Theorem to find $(-1 + \sqrt{3}i)^{12}$

$r = \sqrt{(-1)^2 + (\sqrt{3})^2} = 2$
 $\theta = \tan^{-1}(\frac{\sqrt{3}}{-1}) + 180^\circ$
 $\theta = 120^\circ$

$z^{12} = 2^{12} (\operatorname{cis} 12(120^\circ))$
 $z^{12} = 4096 (\operatorname{cis} 1440^\circ)$

p. 458, #91 (HW)

Roots of Complex Numbers
Fundamental Theorem of Algebra:
of solutions is equal to the degree.

$\sqrt[4]{x^4} = \sqrt[4]{1}$
 $x = \pm 1$
 Double Roots

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Can we find a formula that gives us ALL the roots?

nth Roots of a Complex Number
 The nth roots of a complex number $z=r(\cos\theta+i\sin\theta)$ are given by:

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\theta + 360k}{n} \right)$$

where $k=0, 1, 2, \dots, n-1$

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Example p. 458, #126
 (a) Find the square roots of the given complex number, (b) represent each of the roots graphically, and (c) write each of the roots in standard form.

$16(\cos 60^\circ + i\sin 60^\circ)$

$$\sqrt{z} = \sqrt{16} \left(\cos \frac{60 + 360k}{2} \right)$$

k	roots
0	$4(\cos 30^\circ)$ $4(\cos 30^\circ)$
1	$4(\cos 210^\circ)$ $4(-\frac{\sqrt{3}}{2} - \frac{1}{2}i)$ $-2\sqrt{3} - 2i$

$4(\cos 30^\circ + i\sin 30^\circ)$
 $4(\frac{\sqrt{3}}{2} + \frac{1}{2}i)$
 $2\sqrt{3} + 2i$

$4(\cos 210^\circ + i\sin 210^\circ)$
 $4(-\frac{\sqrt{3}}{2} - \frac{1}{2}i)$
 $-2\sqrt{3} - 2i$

p. 458, #125 (HW)

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Example 8 p. 455
 Find the three cube roots of $z = -2 + 2i$

$r = \sqrt{(-2)^2 + (2)^2} = 2\sqrt{2} = \sqrt{8}$
 $\theta = \tan^{-1}(\frac{2}{-2}) + 180 = 135^\circ$

$$\sqrt[3]{z} = \sqrt[3]{\sqrt{8}} \left(\cos \frac{135 + 360k}{3} \right)$$

k	Root
0	$\sqrt{2}(\cos 45^\circ)$
1	$\sqrt{2}(\cos 165^\circ)$
2	$\sqrt{2}(\cos 285^\circ)$

$\sqrt{2} \cdot \sqrt{2} \cdot \sqrt{2}$

p. 458, #129 (HW)

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HOMEWORK
 ...due Monday along with 6.5a and 6.4-6.5 Partner Quiz

6.5b (p. 458): 91-105 (odd), 113, 115, 125-131 (odd), 141, 143

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