

Grade your own (in pen). Each problem is worth 2 points, for a total of 10 points. Turn in corrections on a new sheet of paper by tomorrow (Friday). Corrections must display all work.

$$1) 125^{-2v-3} = 625^{-2v}$$

$$\left\{ \frac{9}{2} \right\}$$

$$5) 7 \cdot e^{x-2} = 53$$

$$4.0244$$

$$9) \log_4 2x^2 - \log_4 2 = 2$$

$$\{4, -4\}$$

One point for each

$$13) \ln 4 - \ln(x-1) = \ln 24$$

$$\left\{ \frac{7}{6} \right\}$$

$$16) \log_7 x - \log_7(x+1) = 1$$

No solution.

## My Favorite Mistake...

Solve the equations algebraically. Round your results to 3 decimal places.

$$\begin{aligned}\frac{500e^{-x}}{500} &= \frac{300}{500} \\ \ln e^{-x} &= \ln \frac{3}{5} \\ \frac{-x}{-1} &= \frac{\ln(\frac{3}{5})}{-1} \\ x &\approx .511\end{aligned}$$

$$\begin{aligned}\log_4 x - \log_4 (x-1) &= \frac{1}{2} \\ \log_4 \frac{x}{x-1} &= \frac{1}{2} \\ 4^{\frac{1}{2}} &= \frac{x}{x-1} \\ (x-1) 2 &= \frac{x}{x-1} \cdot x-1 \\ 2x-2 &= x \\ x &= 2\end{aligned}$$

$$\frac{500e^{-x}}{500} = \frac{300}{500}$$
$$e^{-x} = \frac{3}{5}$$
$$\ln e^{-x} = \ln \frac{3}{5}$$
$$-x = -.511$$
$$\boxed{x = 0.511}$$

$$\log_4 x - \log_4 (x-1) = \frac{1}{2}$$
$$\log_4 \left( \frac{x}{x-1} \right) = \frac{1}{2}$$
$$4^{1/2} = \frac{x}{x-1}$$
$$2 = \frac{x}{x-1}$$
$$2x - 2 = x$$
$$\boxed{x = 2}$$

**3.5: Using Exponential and Log Equations to Model Data--very cool.**

$$y = ae^{bx}$$
$$A = Pe^{rt}$$

//exponential growth

$$y = ae^{bx}$$

//exponential decay

$$y = ae^{-bx}$$

To find the "mother equation," you must find the values for a and b.

a= initial value

b= rate of growth or decay

**Example** | p. 233, #24

Find the exponential model  $y = ae^{bx}$  that goes through the points  $(0, 1/2)$  and  $(4, 5)$ .

$$\frac{1}{2} = ae^{b \cdot 0}$$

$$\frac{1}{2} = ae^0$$

$$\frac{1}{2} = a$$

$$y = \frac{1}{2}e^{bx}$$

$$5 = \frac{1}{2}e^{4b}$$

$$\ln 10 = \ln e^{4b}$$

$$\frac{\ln 10}{4} = \frac{4b}{4}$$

$$0.576 = b$$

$$y = \frac{1}{2}e^{0.576x}$$

**Example** | p. 233, #12  $y = ae^{bx}$

You invest \$300 in a bank account and 10 years later you have a total of a whopping \$385.21. What was the interest rate? How long will it take for your money to double?

Interest rate

$$\frac{385.21}{300} = \frac{300e^{10b}}{300}$$

$$\ln 1.284 = \ln e^{10b}$$

$$\frac{\ln 1.284}{10} = \frac{10b}{10}$$

$$.025 = b$$

$$2.5\%$$

Double

$$\frac{600}{300} = \frac{300e^{.025X}}{300}$$

$$\ln 2 = \ln e^{.025X}$$

$$\frac{\ln 2}{.025} = \frac{.025X}{.025}$$

$$X = 27.726 \text{ yrs}$$

p. 232, #9 (HW)

**Example**

$$y = ae^{bx}$$

The radioactive element carbon-14 has a half-life of 5730 years. The percentage of carbon-14 present in the remains of plants and animals can be used to determine age. Archaeologists found that the linen wrapping from one of the Dead Sea Scrolls has lost 22.3% of its carbon-14. How old was the linen wrapping?

$$100 - 22.3 = 77.7$$

$$\begin{aligned} & \frac{b}{-5730} \cdot 5730 \\ .5a &= a e^{-5730b} \\ \ln .5 &= \ln e^{-5730b} \\ \ln .5 &= \frac{-5730b}{-5730} \\ -1.2097 \times 10^{-4} &= b \end{aligned}$$

$$\begin{aligned} & \frac{x}{-1.2097 \times 10^{-4}} \\ .777a &= a e^{-1.2097 \times 10^{-4}x} \\ \ln .777 &= \ln e^{-1.2097 \times 10^{-4}x} \\ \ln .777 &= -1.2097 \times 10^{-4}x \\ 2085 \text{ yrs} &= x \end{aligned}$$

# **HOMEWORK**

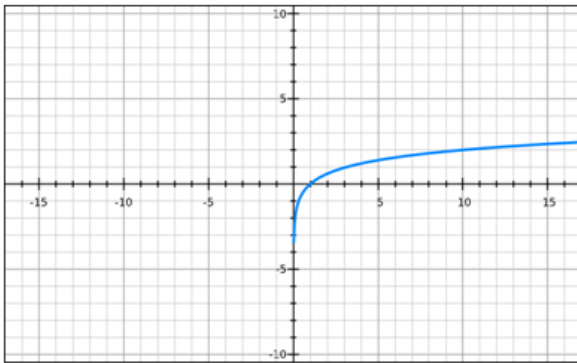
**...apply that math!**

**3.5 (p232): 7-15 odd; 19-25 odd, 29, 35, 39, 43**

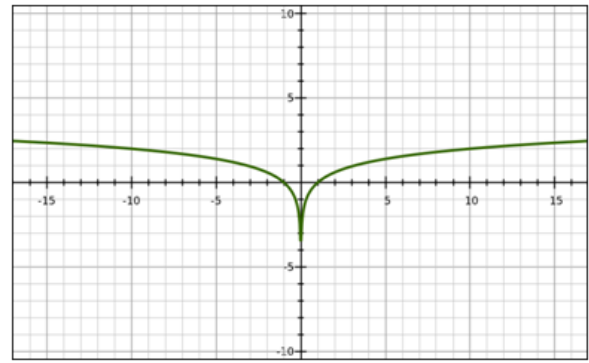


**True or false:**  $\log x + \log x = \log x^2$

True or false:  $\log x + \log x = \log x^2$



$$f(x) = \log x + \log x$$



$$f(x) = \log x^2$$

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The image shows a screenshot of a YouTube video player. The main video is titled "Sherlock Season 1 - Trailer" by the channel "KinologPL", which has 110 videos and 233 subscribers. The video has 124,217 views, 251 likes, and 8 dislikes. It was uploaded on Oct 19, 2011. The video player shows a scene with a large, white, smoke-like cloud in a field. The video progress is at 0:01 / 1:45. To the right of the main video is a list of recommended videos:

- Sherlock Season 2 - Trailer** by KinologPL, 39,762 views, 0:46 duration.
- ShErLoCk CoMeDy ReLiEF** by BtacksGodDaughter, 837,318 views, 10:38 duration.
- Favorite BBC Sherlock moments** by ImMckenzieAKilljoy, 204,650 views, 3:28 duration.
- Top 10 Sherlock Moments (MAJOR SPOILERS)** by Matt Herbert, 188,329 views, 4:44 duration.
- 300: Rise of an Empire Trailer 2013 Official Teaser - 2014 Movie [HD]** by StreamingTrailer, 21,828,928 views, 2:22 duration.
- Sherlock Holmes | The Case Of Violet Smith | Season 1 Episode 1 | FULL** by fanfilmsUK, 77,764 views, 40:01 duration.
- Sherlock: A Scandal in Belgravia Q&A** by BritishFilmInstitute, 331,078 views, 10:29 duration.

Finish your version of the story on a Word document (each group only needs one post). Gold stars will be awarded for incorporating students, teachers, and/or principals. Gold stars will also be awarded if written in the original Sherlock Holmes style. I'm looking for high entertainment value here.

**The first line of your story should give the title as well as the authors.  
Save your document as the first name of each author as well as your hour.**

Title: Sherlock Hearts Calculus by John Doe and Jane Smith  
Save as: John and Jane 3rd hour

Any math should be centered and bolded:

$$\mathbf{T(t)=Ts+(Ts-T_0)e^{(-kt)}}$$

Posts must be submitted before Tuesday's class.

**A sample writing: <http://yep.it/hhmm> where **hhmm** is the time of death.  
For example, if the time of death is 8:45, then go to <http://yep.it/0845>**

<b>Criteria</b>	<b>Possible points</b>
Identified correct time of death (to nearest quarter hour)	1
Identified correct murderer	1
Incorporated at least five lines of mathematics and formatted equations correctly	2
Entertainment Value	1
<b>Total Points</b>	<b>5</b>

$$T - T_s = (T_0 - T_s)e^{-kt}$$

**"...when you have eliminated all which is impossible, then whatever remains, however improbable, must be the truth."**

**Sherlock Holmes Quote, The Blanched Soldier**



Sample Work:

<http://www.ncsec.org/team3/teachers/corpse.html>